

# Event-based Control and Filtering of Networked Systems: A Survey

Lei Zou<sup>1</sup>      Zi-Dong Wang<sup>1,2</sup>      Dong-Hua Zhou<sup>1,3</sup>

<sup>1</sup>College of Electrical Engineering and Automation, Shandong University of Science and Technology, Qingdao 266590, China

<sup>2</sup>Department of Computer Science, Brunel University London, Uxbridge, Middlesex, UB8 3PH, UK

<sup>3</sup>Department of Automation, Tsinghua National Laboratory for Information Science and Technology, Tsinghua University, Beijing 100084, China

**Abstract:** In recent years, theoretical and practical research on event-based communication strategies has gained considerable research attention due primarily to their irreplaceable superiority in resource-constrained systems (especially networked systems). For networked systems, event-based transmission scheme is capable of improving the efficiency in resource utilization and prolonging the lifetime of the network components compared with the widely adopted periodic transmission scheme. As such, it would be interesting to 1) examining how the event-triggering mechanisms affect the control or filtering performance for networked systems, and 2) developing some suitable approaches for the controller and filter design problems. In this paper, a bibliographical review is presented on event-based control and filtering problems for various networked systems. First, the event-driven communication scheme is introduced in detail according to its engineering background, characteristic, and representative research frameworks. Then, different event-based control and filtering (or state estimation) problems are categorized and then discussed. Finally, we conclude the paper by outlining future research challenges for event-based networked systems.

**Keywords:** Event-triggered transmission, networked systems, event-based control, event-based filtering, event-triggered distributed state estimation, distributed control with event-based protocol.

## 1 Introduction

### 1.1 Engineering background

With the progress in networked communication technology the data transmissions among system components in a wide range of applications are implemented via communication networks. Such systems are known as networked systems and they possess many advantages including low cost, simple installation, reduced system wiring, ease of maintenance, high flexibility and reliability. Hence, networked systems have gained ever-increasing research attention in the past few decades. Related to this core area are the control and filtering problems which have attracted considerable research interest<sup>[1–8]</sup>.

The main difference between traditional systems (non-networked systems) and networked systems is the communication process. Data exchanges between components (e.g., signal transmissions between sensors and the controller) are implemented via point-to-point communication in which the components are connected by their corresponding com-

munication channels. However, in networked systems, all signals of various components are transmitted via a shared network (or shared networks). Generally speaking, the communication processes of networked systems could be divided into two categories: time-driven communication and event-driven (or event-based) communication. Time-driven communication is a widely used communication strategy in which the signal transmissions are always implemented in a periodic manner. Such a manner does have the advantages of easy implementation and good predictability. However, in the case that the communication resources (e.g., bandwidth of the network) are the major concern, time-driven communication becomes less preferable since such a communication manner would lead to unnecessary data transmissions. This is particularly true for large scale networked systems with limited communication bandwidth and computation capacity. As such, the event-driven communication appears with the hope to avoid unnecessary signal transmissions<sup>[9, 10]</sup>. Such a communication scheme is capable of improving the efficiency in communication resource utilization and prolonging the lifetime of network components.

In event-driven communication scheme, transmission instants are determined by the so-called “event generator” by which the signal transmission is triggered only when certain triggering condition (i.e., event-triggering condition) is achieved. The triggering condition could be regarded as an index indicating whether the system performance under

Review  
Manuscript received October 18, 2016; accepted December 20, 2016; published online May 4, 2017  
This work was supported by National Natural Science Foundation of China (No. 61329301), the Royal Society of the UK, the Research Fund for the Taishan Scholar Project of Shandong Province of China, the China Postdoctoral Science Foundation (No. 2016M600547), and the Alexander von Humboldt Foundation of Germany.  
Recommended by Editor-in-Chief Guo-Ping Liu  
© Institute of Automation, Chinese Academy of Sciences and Springer-Verlag Berlin Heidelberg 2017

consideration is getting worse than the requirement (e.g., the system becomes unstable). As such, the event-driven communication could provide a trade-off between the system performance and the communication bandwidth utilization. Compared with the time-driven communication scheme, the event-driven communication possesses the features such as aperiodic transmission manner, high communication utilization efficiency and energy saving. So far, the analysis and synthesis issues for networked systems with event-driven communication scheme have gained a great deal of research attention, see e.g., [11–21] and the references therein.

### 1.2 Theoretical frameworks

Event-triggering conditions play an important role in the analysis and synthesis issues of event-driven networked systems. An event-triggering condition is composed of two parts: the error-based part which contains the difference between the current measurement data and the previously transmitted measurement data, and the threshold part. According to the utilization of threshold part in event-triggering mechanisms, there are two different types of event-triggering conditions widely investigated in the literature: the fixed threshold condition<sup>[22–28]</sup> and the relative threshold condition<sup>[11, 12, 16, 17]</sup>. Specifically speaking, let  $y(t)$  and  $t_k$  be the current measurement and the time of the  $k$ -th triggering instant, respectively. In most of the literature, the error-based part  $\delta_e$  is always constructed by  $\delta_e \triangleq (y(t) - y(t_k))^T Q (y(t) - y(t_k))$  where  $Q$  is the weight matrix, the threshold parts  $\rho_t$  of the fixed threshold condition and the relative threshold condition are constructed by  $\rho_t \triangleq r$  and  $\rho_t \triangleq r y^T(t_k) Q y(t_k)$  (where  $r$  is the triggering parameter), respectively. Then, the  $(k + 1)$ -th triggering instant would be determined by  $t_{k+1} \triangleq \{t | t > t_k, \delta_e \geq \rho_t\}$ . Obviously, the parameter  $r$  could regulate the transmission frequency (or communication rate) of the event-triggering mechanism. When  $r$  is set to be zero, the corresponding event-driven system reduces to the conventional time-driven one.

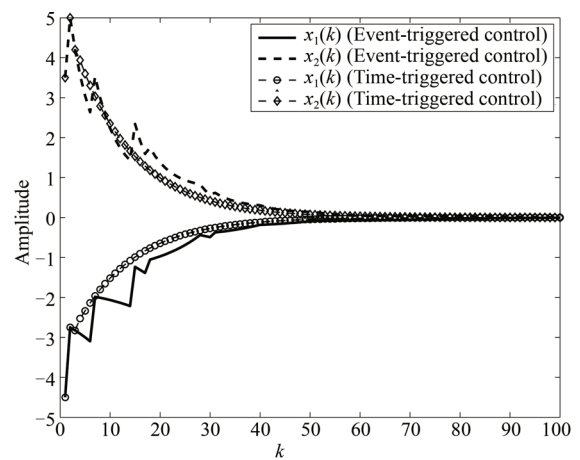
**Remark 1.** Different event-triggering conditions would lead to different control (or filtering) performance. For example, the event-triggering mechanism with a fixed threshold condition (also called “send-on-delta” strategy) is more suitable for the state estimation problem proposed in [24]. Based on the Luenberger estimator and the fixed threshold condition, the estimation error dynamics could be described by an autonomous system, while the relative threshold condition would lead to a non-autonomous system. On the other hand, as shown in [16], the event-triggering mechanism with the relative threshold condition is more suitable for control problems. A properly designed relative threshold condition could guarantee the global asymptotical stability of the closed-loop system.

For the purpose of demonstrating the effectiveness of the event-driven communication, a comparative example of event-triggered control and time-triggered control is presented as follows. The plant is a second-order system which

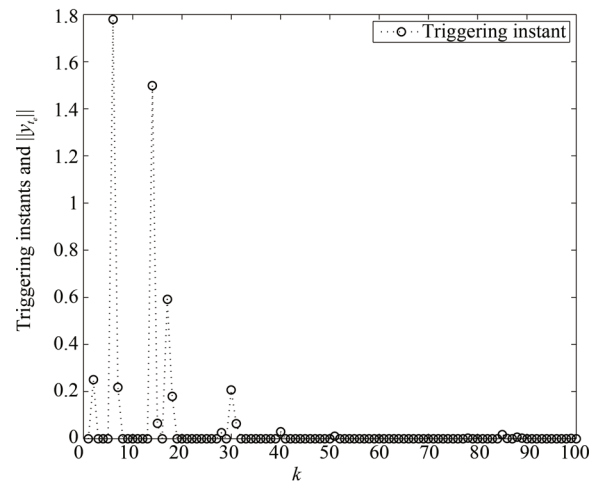
is described by

$$\begin{cases} x_{k+1} = \text{diag}\{1.1, 0.8\}x_k + \begin{bmatrix} 1 & 1 \end{bmatrix}^T u_k \\ y_k = \begin{bmatrix} 1 & 0.5 \end{bmatrix} x_k. \end{cases}$$

In time-triggered control scheme, the control input is set to be  $u_k = -0.8y_k$ . In event-triggered control scheme, the control input and the event-triggering condition is selected as  $u_k = -0.8y_k$  and  $\|y_k - y_{t_s}\| \geq 0.8\|y_k\|$ , respectively. Fig. 1 (a) shows the control performance of event-triggered control and time-triggered control. Fig. 1 (b) describes the transmission instants of the event-driven communication. Obviously, the event-triggering mechanism trades off the communication rate and control performance.



(a) Control performance of different communication schemes



(b) Transmission instants of the event-driven communication

Fig. 1 A comparative example of event-triggered control and time-triggered control

For a networked system with event-based communication mechanism, the dynamics analysis would be inevitably complicated. Traditional approaches are not competent to handle the analysis issue of a networked system with event-based communication. This is mainly due to the aperiodicity of the event-triggered transmission scheme which would

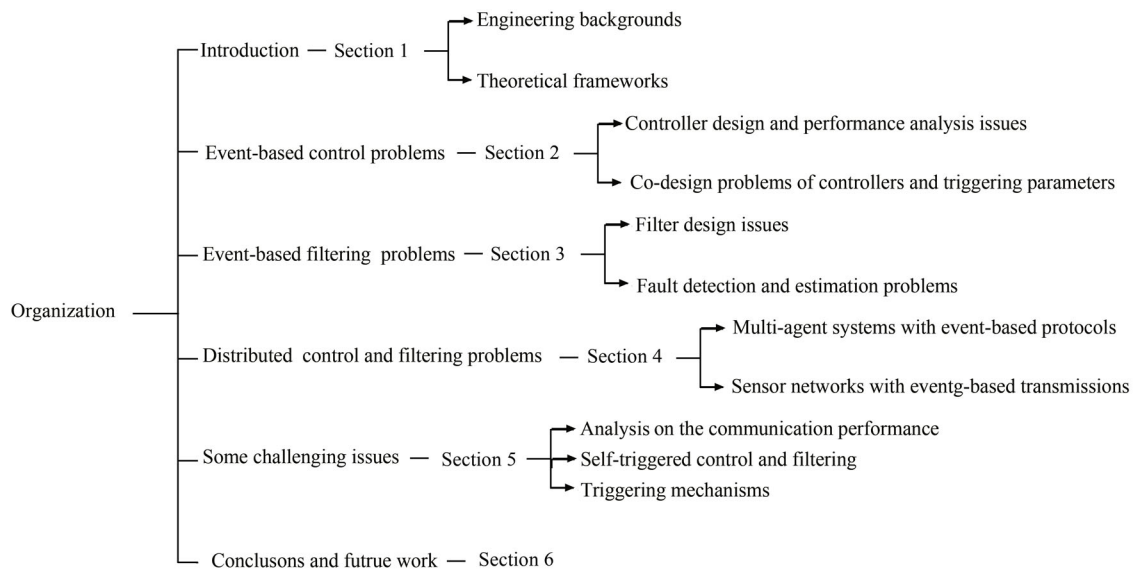


Fig. 2 Organization of this survey

greatly affect the system performance such as the stability and  $H_\infty$  performance of the closed-loop system. In order to deal with such a system, one should consider the system dynamics and the impact of event-based communication simultaneously. More specifically, the corresponding theoretical framework should demonstrate the systems dynamics and the effect induced by the event-triggering condition. Nowadays, three arguable representative theoretical frameworks (e.g., the Lyapunov stability based approach<sup>[14, 17, 29]</sup>, hybrid system based approach<sup>[11, 12]</sup> and input-to-state stability (ISS) based method<sup>[16, 30, 31]</sup>), have been widely applied to deal with the analysis and synthesis problems with event-based communication schemes for networked systems.

Lyapunov stability based approach has been widely employed in the performance analysis and controller (or filter) design. Based on such an approach, the event-triggering condition could be regarded as a nonlinear constraint. Hence, we can embed this nonlinear constraint into the calculation of Lyapunov function or functional. Obviously, such an approach could be considered as the “robustness-based” method. On the other hand, by substituting the error-based part into the system dynamics, the event-driven system could be reformulated as a dynamical system with an input  $(y(t) - y(t_k))$  satisfying the bounded constraint induced by the utilized event-triggering condition. Then, the ISS based method could be applied to cope with the analysis and synthesis issues for the reformulated system. Compared with the Lyapunov stability based approach and the ISS based method, hybrid system based approach is introduced based on the fact that the event-driven system could be reformulated by a dynamical system with the impulsive behavior. Hence, we can analyze the dynamical behaviors of such a system via the hybrid system based approach.

This survey aims to provide a timely review on the recent advances of the event-based control and filtering prob-

lems for networked systems. The references discussed in this paper include, but are not limited to the following aspects of networked systems: 1) stability analysis problem of networked systems with event-based communication, 2) methods and algorithms to design event-based controller and event-based filter for networked systems, 3) robustness analysis issue of event-driven networked systems, and 4) distributed control and state estimation problems with event-based transmission scheme. The organization of this survey could be summarized by Fig. 2. In the following sections, the developments of the distributed event-based control for multi-agent systems (MASs) and the distributed event-based state estimation for sensor networks (SNs) are systematically reviewed as follows.

## 2 Event-based control problems

Typical event-driven networked control systems (NCSs) could be categorized into two groups, which are demonstrated by Fig. 3. In this section, we will recall the theoretical developments of event-based control issues in the recent years from various aspects including the controller design and performance analysis, and the co-design issues of controllers and triggering parameters.

**Remark 2.** In NCSs, both the sensor-to-controller channel and the controller-to-actuator channel could be implemented via communication networks. For example, in [32], the stabilization problem has been studied for NCSs with both-sides networks. Hence, in order to reduce the communication burden of both-sides networks, the event-triggering mechanism could be utilized in both the sensor-to-controller channel and the controller-to-actuator channel (e.g., [33, 34]). On the other hand, when the network resource of the sensor-to-controller channel is the only concern, the paradigm shown in Fig. 3 (b) is more suitable for the NCS.

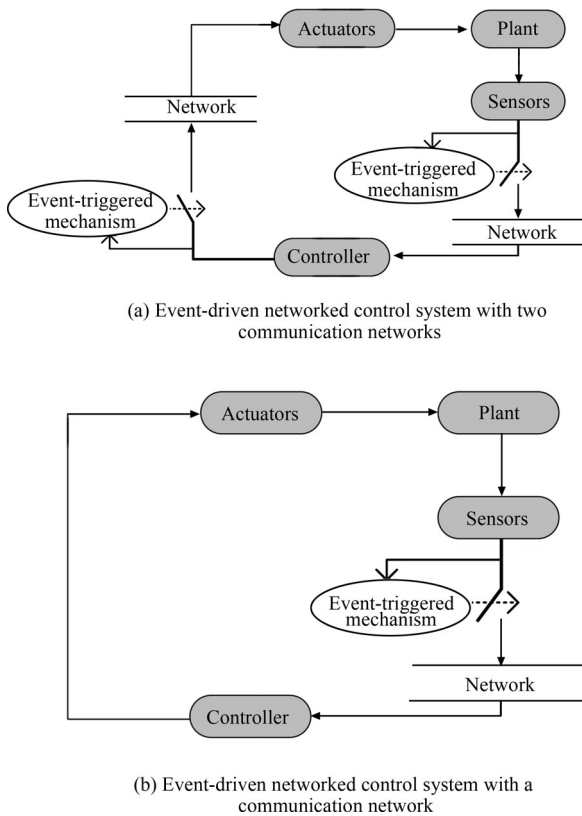


Fig. 3 Two typical event-driven networked control systems

## 2.1 Controller design and performance analysis issues

$H_\infty$  control is one of the most investigated control problems due to its wide applications in various control systems. A rich body of literature has appeared on the  $H_\infty$  controller design issue subject to time-driven communication. With respect to the analysis and design issue of controller subject to event-triggered transmission scheme, the time-triggered controllers are extremely difficult to handle the control task with the satisfactory performance. As such, a great deal of research attention has been devoted to the event-based  $H_\infty$  control issue in recent years, e.g., [35–38]. In [39], the  $H_\infty$  control problem has been investigated for a class of NCSs based on event-time-driven model. By reformulating the considered systems into a class of switched delay systems including an unstable subsystem, the switching controller has been designed in terms of linear matrix inequalities (LMIs). The  $H_\infty$  control issue has been studied in [40] for a class of discrete-time linear parameter-varying systems with network-induced delays. In [41], the  $H_\infty$  tracking control design problem has been studied for a class of continuous-time NCSs with event-triggered sampling scheme. With respect to the control problem with communication delay, we mention some representative work as follows. In [29], a delay system model has been firstly constructed for the analysis of NCSs with event-triggered communication. Note that the presented event-triggered communication is imple-

mented based on the sampled data of sensors. A combined event-triggering condition and controller-feedback-gain design approach has been presented in [17] for NCSs, where the communication delay and packet loss phenomenon have been taken into consideration. Hu et al.<sup>[42]</sup> illustrated the event-triggered  $H_\infty$  stabilization (in mean square sense) problem for NCSs with multiplicative noise and network-induced delays. Markov jump system has a wide range of application because of its capacity of capturing the abrupt mode changes of the plant. In [43], the event-based  $H_\infty$  control problem has been dealt with for discrete Markov jump systems based on a time interval analysis approach. The event-triggered  $H_\infty$  controller design problem has been investigated in [44] for nonlinear NCSs with time delay and uncertainties, where the uncertainties in networked Takagi-Sugeno (T-S) fuzzy model have been modeled by the parallel distributed compensation fuzzy control rules.

$L_\infty$  control has long been a hot topic in control theory. In [11], the stability and  $L_\infty$ -performance have been studied for event-triggered control systems with dynamical output-based controllers and decentralized event-triggering mechanisms via an impulsive system based method. The stabilization of the event-based networked systems subject to both quantization and time-varying network induced delay has been address in [45] where both fixed threshold condition and relative threshold condition have been considered simultaneously. In [46], a novel event-triggered control strategy called rollout event-triggered control has been developed which is capable of guaranteeing a performance improvement over traditional periodic control for cyber-physical systems. The main results established in that paper have quantified the performance improvements for quadratic average cost problems. The event-based pinning control problem for the synchronization of complex networks has been investigated in [47] where the considered networks have been modeled by time-varying weighted graphs and featuring generic linear interaction protocols. The event-based sampled-data model predictive control problem has been studied in [48] based on the non-monotonic Lyapunov function approach for continuous-time systems with disturbances. With respect to the spatially distributed system, in [49], an event-based model predictive networked control scheme has been proposed for a traffic control system (which has been modeled as a spatially distributed system). As it is well known, the distributed parameter systems could be modeled by partial differential equations (PDEs). The event-triggered control problem has been studied in [50] for parabolic systems (a class of distributed parameter systems) governed by semi-linear diffusion PDEs with transmission delays and signal quantization.

Optimal control is another hot topic in control theory dealing with the problem of finding a control law for a given system such that a certain optimality criterion is achieved. A local event-based approach has been developed in [51] for the optimal control of the heating, ventilation, and air-

conditioning (HVAC) systems, where decisions were made only when certain events occurred. On the other hand, the suboptimal event-triggered control problem has been considered in [52] for delay linear systems where the performance considered has included a linear quadratic cost function for quantifying the control performance and average event times. In [53], the fault-tolerant control problem has been discussed for networked systems with dynamic quantization and event-triggered transmission scheme. The semi-global stabilization problem has been studied in [54] for null controllable systems with actuator saturation and event-triggered transmission scheme via Riccati equations. In [55], a novel approximation-based event-triggered control scheme has been proposed for multi-input multi-output uncertain nonlinear continuous-time systems in affine form. A nonzero positive lower bound of the inter-event times is guaranteed to avoid the Zeno behavior (i.e., the occurrence of an infinite number of events in finite time).

## 2.2 Co-design of controllers and triggering parameters

The main idea of the co-design problem of event-based control and triggering condition is to design the desired controller parameters and certain parameters of the event-triggering mechanism simultaneously. Up to now, such a problem has received a great deal of research interest in the literature. In [12], the co-design problem has been presented for a linear time-invariant continuous-time system with the periodic event-triggered controller. Both the static state-feedback and dynamical output-based controllers have been considered. Furthermore, three different approaches (e.g., impulsive system based approach, piecewise linear system based method, and perturbed linear system based method) to cope with such a problem have been presented and discussed. The model-based event-triggered predictive control problem has been investigated in [56] for discrete-time linear systems with time-varying communication delays, where the co-design problems of the controller and the event-triggering parameter have been discussed in terms of the linear matrix inequality approach and the Lyapunov functional method. Al-Areqi et al.<sup>[57, 58]</sup> studied the co-design problems of event-based control and scheduling for networked embedded control systems (NECSs) in which multiple control loops closed over a communication network have been implemented on embedded processors. By modeling the considered systems as discrete-time switched linear systems, the co-design issues have then been formulated as certain LMI optimization problems with associated quadratic cost functions. A novel event-triggering mechanism (dynamic triggering mechanism) has been introduced in [59]. The co-design problem addressed there was to design the corresponding event-triggering parameters and feedback controller so that the resulting closed-loop systems could keep stable.

The co-design problem of dynamic output feedback con-

troller and event-triggering parameters have been proposed in [60] with data quantization. Two design approaches have been presented for both event-triggered sampled output-feedback case and periodic event-triggered output feedback case via a hybrid system model based framework. The small-gain approach has been applied in [61, 62] to cope with the design problems of event-triggering parameters for networked nonlinear systems. First, the closed-loop system under consideration has been reformulated as two subsystems. Based on the reformulation, the Lyapunov-based small-gain theorems have been utilized to design the triggering conditions. In [63], the co-design problem of output tracking controller and event-triggering parameters has been studied for a T-S fuzzy system. The resulting system has been modeled as an asynchronous threshold-error-dependent T-S fuzzy system with time-varying delay. The co-design problems of event-triggering parameters and controllers for sampled-data systems have been discussed in [64, 65]. Specifically, in [64], the  $L_2$  control problem has been studied and criteria have been derived for the system analysis and synthesis by using the saw tooth structure characteristic of an artificial delay. In [65], the event-triggered transmission scheme has been considered in both sensor-to-controller network and controller-to-actuator network. Furthermore, both static output feedback control and dynamic output feedback control have been studied simultaneously. In [66], a non-fragile control system approach has been employed to design the event conditions in event-triggered control systems. It has been shown that the designed event condition would be less conservative and leads to larger inter-event times than the event conditions in some existing works.

## 3 Event-based filtering problems

State estimation and filtering problems are widely used in real engineering applications to reconstruct the system state of the plant from measurements with external disturbances. A typical event-driven filtering system is shown in Fig. 4. In this section, we will review the developments of the event-based filtering and state estimation as follows.

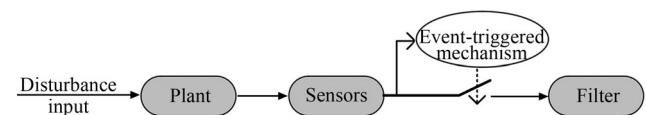


Fig. 4 A typical event-driven filtering system

### 3.1 Filter design issues

Recursive filtering technology is an effective tool for estimating the states of a system and has attracted significant research attention due to the widespread success of the Kalman filter in industrial applications (especially in aerospace application). In [67], an event-based sensor data scheduler has been proposed. Then, a modified recursive filter (i.e., minimum mean-squared error (MMSE) estimator)

has been derived as well as an approximate estimator under the event-based sensor data scheduler. The networked estimation problem with modified send-on-delta transmission method has been investigated in [25]. In the proposed transmission method, an event-based sampling has been utilized combined with a time-triggered sampling scheme to detect packet dropouts. The structure of such a recursive filter has also been studied in [68] based on the event-based sampling scheme. The corresponding estimation performance has been analyzed under such a sampling scheme. In [69], the optimal sensor fusion problem has been studied based on the hybrid measurement information provided by a sequence of sensors.

Different from previous triggering mechanisms, a novel event-triggering mechanism called variance-based triggering scheme has been developed in [70], where the event-based state estimation problem has been considered for a stochastic linear time-invariant system. In [71], the event-based sampling strategies (e.g., send-on-delta and matched sampling) have been introduced in detail. Then, the set-membership property of the proposed triggering criteria has been derived. A modified state estimator has been developed based on the proposed set-membership measurement information. In [72], an event-based recursive filter has been developed for discrete time-varying systems with fading channels, randomly occurring nonlinearities and multiplicative noises via the recursive linear matrix inequality approach. In [73], the properties of set-valued Kalman filters with multiple sensor measurements have been explored. Furthermore, the obtained results have been applied to the event-based estimation, which could be regarded as the event-based MMSE estimation algorithm.

Recursive filtering (e.g., Kalman filtering and extended Kalman filtering) is capable to deal with the state estimation tasks with Gaussian noise. However, sometimes, accurate system models are not as readily available and the noise in many practical filtering problems is non-Gaussian. In this case, a variety of filtering algorithms have been proposed to cope with such problems. One of the most investigated one is the  $H_\infty$  filtering approach. In [74], the  $H_\infty$  filtering problem has been investigated for networked systems with an event-triggered scheme. The online scheduling strategy has been proposed based on a novel middleware in which two modules (e.g., information selection module and congestion avoidance module) have been developed. The event-based  $H_\infty$  filtering problem has been studied in [14] for networked systems with communication delay, where a new model of filtering error system has been established via a novel delay system approach with simultaneous consideration of communication delay and event-triggered scheme. By applying the Lyapunov-Krasovskii functional method combined with free weighting matrix approach, in [75], a periodic event-triggered  $H_\infty$  filter design approach has been provided for a discrete linear system. In the proposed periodic event-triggered communication scheme, the sensor has been time-triggered and the transmitter has been

event-triggered in a periodic manner with the known sampling period. Then, the  $H_\infty$  filtering analysis criterion and stabilization criterion are obtained in terms of LMIs. The communication and filtering parameters have been acquired based on a co-design algorithm in a unified framework.

With respect to the sampled data systems, the event-based  $H_\infty$  filtering problem has been examined in [76, 77]. An event-based bounded real lemma has been formulated to co-design the  $H_\infty$  filters and the event parameters for the sampled-data system by employing the Lyapunov-Krasovskii functional approach. In [78], the event-based filtering problem has been studied for discrete time-varying systems in a finite-horizon. Based on the predefined event-triggered scheme, the corresponding structure of the time-varying filter has been introduced. The adaptive event-based  $H_\infty$  filtering problem has been studied in [79] for a class of T-S fuzzy systems with time delay, where the threshold of the event-triggering mechanism could be adaptively adjusted. In [80], the problem of event-triggered  $H_\infty$  filtering for networked Markovian jump system has been investigated where a dynamic discrete event-triggered scheme has been designed. A co-design scheme for the  $H_\infty$  filter and event-triggering parameters has been proposed. The event-triggered  $H_\infty$  filtering issue has been addressed in [81] for networked T-S fuzzy systems with the asynchronous constraints of the membership functions. It could be observed that the asynchronous constraints on membership functions could reduce the conservativeness of the filter design and achieve a better  $H_\infty$  performance.

### 3.2 Fault detection and estimation

The study on fault diagnosis is an important and challenging problem in a variety of communities including chemical engineering, nuclear engineering and automotive systems. Generally speaking, there are three different research areas for fault diagnosis: 1) fault detection (FD), 2) fault isolation (FI), and 3) fault estimation. The aim of FD is to design a residual generator based on which a decision can be made to judge whether a fault occurred. Because of the rapid developments in networked control systems (NCSs), increasing research attention has been devoted to the FD problem subject to networked environment. In [82], the event-based FD problem has been examined for a class of networked systems subject to communication delay and nonlinear perturbation. A novel event-triggered transmission scheme has been introduced with the hope to reduce the communication load. Under the proposed event-triggered transmission scheme, the event-based FD model has been developed with the consideration of network transmission delay. The general structure of the event-triggered FD algorithm has been introduced for networked control systems in [83] where the proposed event-triggered FD algorithm was compatible with various event-triggered schemes. Then, the proposed algorithm has been applied for FD of the NCS under the mixed event-triggering mechanism. Furthermore, a similar design problem has been con-

sidered where the FD algorithm was co-implemented with the control algorithm on the same processor. Finally, some concluding remarks have been drawn and some possible future research directions have been pointed out. In [84], the problem of event-triggered FD filter and controller coordinated design has been investigated for a continuous-time NCS with biased sensor faults based on the combined mutually exclusive distribution and Wirtinger-based integral inequality approach.

FI is the next step of FD process. The aim of FI is to determine the location of the fault. In the FI process, in order to enhance the isolability of the faults, the residuals should be generated with directional properties in response to a particular fault. The FI problem subject to event-triggered sampling scheme has been studied in [85] for linear stochastic systems with multiple faults. According to the proposed send-on-delta sampling scheme, a modified fault isolation filter has been developed based on a particular form of the Kalman filter. For the purpose to provide an estimation of the faults, an event-triggered fault estimator has been designed in [86] for a class of nonlinear systems. For the purpose of characterizing the features of communication network, the event-triggered transmission scheme and missing measurements phenomenon have been considered simultaneously. The corresponding fault estimator has

been implemented in the form of extended Kalman filter by which the fault and states can be jointly estimated. The required parameters to be designed have been derived by solving two recursive matrix equations which are suitable for online applications.

#### 4 Distributed control and state estimation problems

Nowadays, most of the real-world large-scale systems could be modeled as networked agent systems, where examples include biological systems, multi-vehicle systems, and distributed sensor systems. For such systems, it might be no longer valid to deal with them via centralized control or centralized state estimation schemes due to the huge requirements on communication resources and computation capability<sup>[87, 88]</sup>. As such, distributed control and state estimation schemes become necessary to deal with such systems. For distributed control and state estimation problems, nodes could exchange their information according to the underlying connection links, in which the event-triggered transmission scheme would lead to certain dynamical behaviors. A typical networked agent system with event-based communication is described by Fig. 5. In this

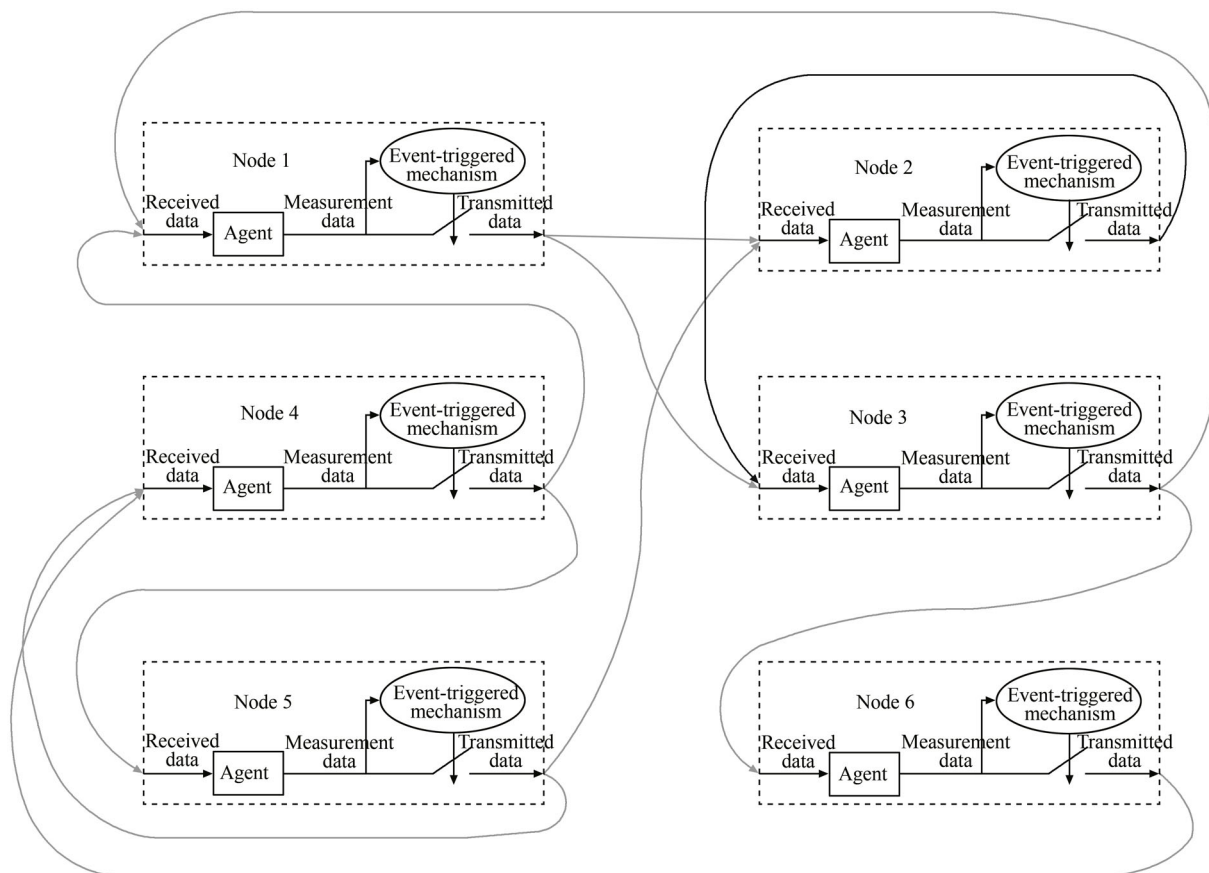


Fig. 5 An event-driven networked agent system with six nodes (RD: received data, MD: measurement data, TD: transmitted data, E-T M: event-triggered mechanism)

section, the developments of the distributed event-based control for multi-agent systems (MASs) and the distributed event-based state estimation for sensor networks (SNs) are systematically reviewed as follows.

#### 4.1 Multi-agent systems with event-based protocols

Consensus problem for MASs has received intensive research attentions in the past decade due primarily to their practical application insights in a variety of fields<sup>[89]</sup>. Chen and Hao<sup>[90]</sup> investigated the event-triggered and self-triggered consensus control schemes for discrete-time MASs, where the event-triggering condition proposed was related to the measurement error and the disagreement vector. The distributed rendezvous problem has been studied in [91] for MASs with event-triggered controllers where a combinational measurement approach has been proposed in the event-based controller design algorithm. Based on such a design, the control of each agent is only triggered at its own event-time which could reduce the amount of signal transmissions between controllers. The event-based consensus control issue with time-dependent triggering conditions has been proposed in [92] in which the asymptotic convergence to average consensus was guaranteed and Zeno behavior was excluded. In [93], an event-based control algorithm has been proposed to achieve the consensus performance for MASs with fixed topology via sampled data. The consensus problem has been studied in [94] for discrete-time heterogeneous MASs with random communication delays represented by a Markov chain and event-triggered control protocols, where the mean square stability of the closed-loop MASs has been studied analyzed based on the Lyapunov functional method and the Kronecker product technique. In [95], the event-triggered transmission scheme has been examined for distributed control systems with packet loss and transmission delays. Intensive analysis has taken place for both linear and nonlinear subsystems via ISS design technology and LMI technology. Sampled data control scheme is a widely used method in networked control systems. In [96], the event-triggered sampled-data consensus problem has been investigated for MASs with directed graph. The MAS-based event-triggered hybrid control problem has been considered in [97] for intelligently restructuring the operating mode of a micro-grid (MG) to ensure the energy supply with high security, stability and cost effectiveness.

In MASs, asynchronous sampling means that the sampling of each agent does not happen at the same time. In [98], the consensus problem has been investigated for first-order MASs under linear asynchronous decentralized event-triggered control scheme, where both the undirected and directed topologies have been considered. The consensus problem has been studied in [99] for MASs with randomly occurring nonlinear dynamics and time-varying delay based on stochastic analysis approach and Kronecker product

technique. Both centralized and distributed event-triggered cooperative control strategies have been proposed in [100] for MASs with linear dynamics based on output feedback control scheme. The leader-following event-triggered asynchronous sampling scheme has been studied in [101] for second-order multi-agent systems. It has been shown that the inter-event intervals are lower bounded by a strictly positive constant, which could exclude the Zeno-behavior. The leader-follower flocking problem has been proposed in [102] for MASs via a new hybrid control algorithm where the signal transmissions are governed by a distributed event-triggering mechanism. In [103], the finite-time distributed event-triggered consensus control problem has been investigated for MASs based on the finite-time stability theory. The event-triggered leader-follower tracking control problem has been studied in [104] for MASs with general linear dynamics for both undirected and directed follower graphs. In [105], the consensus problem has been considered for second-order MASs where the data is sampled randomly and transmitted based on the event-triggering mechanism according to the topology governed by a directed spanning tree. The obtained results have been further extended to other practical control applications where the agents have been equipped with limited capability microprocessor.

#### 4.2 Sensor networks with event-based transmissions

In the past few decades, a rich body of literature has appeared on the distributed state estimation problems for sensor networks (SNs) due mainly to the insight of their engineering applications, see [106–108] and the references therein. It is worth mentioning that the research on event-based state estimation problem is of great importance for SNs since it is usually crucial to ensure the efficient communication and energy consumption. This is particularly true for wireless SNs, where the sensors are battery-operated and communication resources are often a concern. In this case, event-based transmission scheme serves as a natural alternative for the smooth operation of the SNs. In [109], the event-triggered distributed  $H_\infty$  state estimation problem has been investigated for a class of discrete-time stochastic nonlinear systems with packet dropouts in a SN, where the innovation information of each sensor node has been transmitted only when certain triggering condition has been violated. The event-based distributed state estimation problem has been addressed in [110] for nonlinear discrete-time delayed systems over SNs with event-triggered communication scheme. Different from the innovation-based triggering condition proposed in [109], the event-triggering mechanism of [110] is implemented based on the local measurement of each sensor node (i.e., measurement-based triggering mechanism). Based on the innovation-based triggering mechanism, the distributed  $H_\infty$  consensus filtering problem has been studied in [111] for mobile SNs via sampled measurement. A unified co-design algorithm for the filter gains and



triggering parameters has been given. In [112], the distributed state estimation algorithms have been established for linear time-varying discrete-time systems with event-triggered transmission scheme over wireless SNs. Corresponding stability analysis has been proposed. The event-triggered distributed state estimation problem for uncertain stochastic systems with state-dependent noises has been considered in [113], where the norm-bounded uncertainty has been supposed to be occurred in a random way, which has been modelled by the Bernoulli distributed white sequences with known conditional probabilities.

The event-based distributed filtering problem for continuous-time Itô stochastic systems has been investigated in [114] over the wireless SNs subject to finite resources and stochastic measurement fading. An adaptive algorithm for determining the triggering parameter has been developed, by which the intelligent sensors have been allowed to tune the boundary of a local event domain in an online manner. In [115], the recursive distributed filtering technology has been developed for a class of discrete time-varying systems with event-based communication scheme, where the upper bound for filtering error covariance could be computed recursively by solving a Riccati-like matrix equation. The distributed event-based  $H_\infty$  filtering problem has been studied in [116] for continuous-time linear time-invariant systems over SNs with communication delays. In [117], the event-triggered distributed state estimation problem has been considered for a class of discrete nonlinear stochastic systems with time-varying delays, randomly occurring uncertainties and randomly occurring nonlinearities. The estimator has been designed by constructing a Lyapunov-Krasovskii functional and employing the delay-fractioning approach. The Kalman consensus filter has been developed in [118] for linear time-varying systems over SNs with event-triggered transmission scheme in which the triggering decision was based on the send-on-delta data transmission mechanism. The event-based distributed set-membership filtering problem has been investigated in [119] for time-varying nonlinear systems over SNs subject to saturation effects. In [120], the event-triggered distributed filtering algorithm has been presented for non-Gaussian systems over wireless SNs. The boundedness of the presented distributed filter parameter has then been analyzed. In [121], the distributed estimation problem is examined for networked systems with network-induced delays and dropouts as well as the event-based communication scheme. The estimator's structure of each agent is designed based on local Luenberger-like observers with consideration of consensus strategies. The event-triggered distributed state estimation problem is examined in [122] for large-scale systems over a wireless network. A global event-based communication policy is introduced to minimize the weighted function of the network energy consumption and the number of transmissions. The proposed minimization problem is solved based on a distributed 1-step greedy heuristic.

## 5 Some challenging issues

In the past decade, we have witnessed significant progress on the event-based control and filtering issues for various networked systems, and a large number of results have been reported on such topics. In this section, we highlight some challenging problems with respect to these topics.

### 5.1 Analysis on the communication performance

The main idea of event-triggering mechanism is to reduce the signal transmission frequency while guaranteeing a satisfactory system performance. The signal transmission frequency is largely dependent on the threshold of the event-triggering condition. Generally speaking, a big threshold would lead to a low signal transmission frequency. However, it is still difficult to evaluate the exact communication performance of an event-driven networked system. In other words, the "average transmission rate" and the "maximum transmission rate" are still difficult to derive for a networked system with the known event-triggering condition. Shi et al.<sup>[123]</sup> considered the event-triggered state estimation in the framework of maximum likelihood estimation. Furthermore, for the one-step problem, the calculation of upper and lower bounds of the transmission rates from the process side has also been briefly analyzed. In [73], the event-based state estimation problem has been studied where the triggering conditions could be designed by considering requirements on performance and transmission rates. In [67], a minimum mean-squared error estimator has been developed. Moreover, an illustrative relationship between the transmission rate and the estimation quality has been achieved. It should be pointed out that, up to now, the corresponding results concerning the analysis on communication performance are very scattered for event-driven networked systems with different networked-induced effects (e.g., communication delays, quantization effects) due primarily to the difficulty in the mathematical analysis on the effects induced by the event-triggering mechanism.

### 5.2 Self-triggered control and filtering

Event-triggering mechanism is implemented based on the generation of the "event", which requires special hardware to detect the measurement output frequently. The hardware could be realized by application-specific integrated circuits (ASIC) of field-programmable gate array (FPGA) processors. Hence, event-triggering mechanism would inevitably lead to additional cost of energy in order to keep the sensor awake and computing unceasingly. As such, the self-triggered strategy has been explored to "calculate" the transmission instant in the absence of continuous monitoring of the measurement output. The self-triggered mechanism represents a model-based emulation of the event-triggering mechanism by replacing the detection task by certain admissible "prediction", which could be computed by the software. More specifically, the next

triggering instant is precomputed by the previously transmitted data and the knowledge of the system dynamics. In [124], an introductory overview on the event-triggered and self-triggered control problems has been presented. Some existing results on networked systems with self-triggered mechanisms have been reported in [125–128]. However, the corresponding results concerning self-triggered control and filtering problems are very scattered for nonlinear systems and complex systems with various networked-induced phenomena. Furthermore, how to predict the triggering instant with less conservatism is another challenging topic.

### 5.3 Triggering mechanisms

As we introduced in Section 1.2, there are two triggering mechanisms widely adopted in the literature: the fixed threshold triggering and the relative threshold triggering. One of the main difficulties for event-driven networked systems is to design suitable event-triggering mechanism guaranteeing that a positive minimum inter-event time existed (Zeno behavior could be avoided). In [59], a novel event-triggering mechanism named dynamic triggering mechanism has been introduced where an internal dynamic variable satisfying certain differential equation is employed to generate the event-triggering condition. In such a triggering condition, the information about the error-based part from the previous transmission instant to the current time instant has been considered. Such a triggering mechanism has been improved in [129] in which an auxiliary parameter has been added to provide a lower bound on the minimum inter-event time. In [27], a new integral-based event-triggering mechanism has been developed for a class of nonlinear systems. It has been shown that the event-driven system with such a triggering mechanism is more efficient and less conservative than the corresponding system introduced in [16]. So far, the corresponding results concerning other triggering mechanisms (excluding the fixed threshold triggering and the relative threshold triggering) are very scattered. How to develop other suitable triggering mechanism is a challenge topic worthy of further investigation.

## 6 Conclusions and future work

In this paper, we have discussed and reviewed results, mostly from relatively recent work, on the problems of event-based control and filtering for networked systems. Various event-based control problems and event-based filtering (or state estimation) problems have been surveyed in great detail for different networked systems. Based on the literature review, some related topics for the future research work are listed as follows.

1) The main purpose to design the event-based controllers or event-based filters is to provide a trade-off between the system performance and the communication utilization efficiency. Hence, it would be a promising research topic to analyze the relationship between the system performance and the “average transmission rate” induced by

the event-triggering mechanism.

2) So far, two event-triggering mechanisms have been widely studied, e.g., fixed threshold triggering (or send-on-delta triggering) mechanism, and relative threshold triggering mechanism. Some modified event-triggering mechanisms could be further considered (e.g., dynamic triggering mechanism introduced in [59]).

3) Event-triggering mechanism should be implemented based on certain component called “event generator” which would increase the cost of networked systems. As such, self-triggering mechanism becomes an alternative scheme to improve the communication utilization efficiency. Therefore, it leads to a particularly attractive area for developing controllers and filters based on self-triggered transmission schemes.

4) The nonlinearities addressed have some constraints that may bring somewhat conservative results. A trend for future research is to study the co-design problems of event-triggering conditions and controllers (or filters) parameters for nonlinear stochastic systems.

5) Another future research direction is to discuss the applications of the established theories and methodologies to some practical engineering problems such as smart grids and mobile robots.

## References

- [1] E. G. Tian, D. Yue, C. Peng. Reliable control for networked control systems with probabilistic actuator fault and random delays. *Journal of the Franklin Institute*, vol. 347, no. 10, pp. 1907–1926, 2010.
- [2] M. Sahebsara, T. W. Chen, S. L. Shah. Optimal  $H_\infty$  filtering in networked control systems with multiple packet dropouts. *Systems & Control Letters*, vol. 57, no. 9, pp. 696–702, 2008.
- [3] R. Caballero-Águila, A. Hermoso-Carazo, J. Linares-Pérez. Optimal state estimation for networked systems with random parameter matrices, correlated noises and delayed measurements. *International Journal of General Systems*, vol. 44, no. 2, pp. 142–154, 2015.
- [4] D. E. Quevedo, A. Ahlén, A. S. Leong, S. Dey. On Kalman filtering over fading wireless channels with controlled transmission powers. *Automatica*, vol. 48, no. 7, pp. 1306–1316, 2012.
- [5] M. S. Mahmoud. *Control and Estimation Methods over Communication Networks*, London, UK: Springer-Verlag, 2014.
- [6] M. S. Mahmoud. Improved networked-control systems approach with communication constraint. *IMA Journal of Mathematical Control and Information*, vol. 29, no. 2, pp. 215–233, 2012.
- [7] M. S. Mahmoud, M. F. Emzir. State estimation with asynchronous multi-rate multi-smart sensors. *Information Sciences*, vol. 196, pp. 15–27, 2012.
- [8] M. S. Mahmoud, S. Z. Selim, P. Shi, M. H. Baig. New results on networked control systems with non-stationary

- packet dropouts. *IET Control Theory & Applications*, vol. 6, no. 15, pp. 2442–2452, 2012.
- [9] M. S. Mahmoud, M. Sabih. Networked event-triggered control: an introduction and research trends. *International Journal of General Systems*, vol. 43, no. 8, pp. 810–827, 2014.
- [10] M. S. Mahmoud, A. M. Memon. Aperiodic triggering mechanisms for networked control systems. *Information Sciences*, vol. 296, pp. 282–306, 2015.
- [11] M. C. F. Donkers, W. P. M. H. Heemels. Output-based event-triggered control with guaranteed  $\mathcal{L}_\infty$ -gain and improved and decentralized event-triggering. *IEEE Transactions on Automatic Control*, vol. 57, no. 6, pp. 1362–1376, 2012.
- [12] W. P. M. H. Heemels, M. C. F. Donkers, A. R. Teel. Periodic event-triggered control for linear systems. *IEEE Transactions on Automatic Control*, vol. 58, no. 4, pp. 847–861, 2013.
- [13] N. He, D. W. Shi. Event-based robust sampled-data model predictive control: A non-monotonic Lyapunov function approach. *IEEE Transactions on Circuits and systems I: Regular Papers*, vol. 62, no. 10, pp. 2555–2564, 2015.
- [14] S. L. Hu, D. Yue. Event-based  $H_\infty$  filtering for networked system with communication delay. *Signal Processing*, vol. 92, no. 9, pp. 2029–2039, 2012.
- [15] D. V. Dimarogonas, K. H. Johansson. Event-triggered control for multi-agent systems. In *Proceedings of the 48th IEEE Conference on Chinese Control Conference Decision and Control*, IEEE, Shanghai, China, pp. 7131–7136, 2009.
- [16] P. Tabuada. Event-triggered real-time scheduling of stabilizing control tasks. *IEEE Transactions on Automatic Control*, vol. 52, no. 9, pp. 1680–1685, 2007.
- [17] C. Peng, T. C. Yang. Event-triggered communication and  $H_\infty$  control co-design for networked control systems. *Automatica*, vol. 49, no. 5, pp. 1326–1332, 2013.
- [18] M. Mazo Jr., P. Tabuada. On event-triggered and self-triggered control over sensor/actuator networks. In *Proceedings of the 47th IEEE Conference on Decision and Control*, IEEE, Cancun, Mexico, pp. 435–440, 2008.
- [19] F. Forni, S. Galeani, D. Nešić, L. Zaccarian. Event-triggered transmission for linear control over communication channels. *Automatica*, vol. 50, no. 2, pp. 490–498, 2014.
- [20] N. Espitia, A. Girard, N. Marchand, C. Prieur. Event-based control of linear hyperbolic systems of conservation laws. *Automatica*, vol. 70, pp. 275–287, 2016.
- [21] A. M. Memon, M. S. Mahmoud. Evaluation of novel self-triggering method for optimisation of communication and control. *IET Control Theory & Applications*, vol. 10, no. 1, pp. 76–83, 2016.
- [22] E. Garcia, P. J. Antsaklis. Model-based event-triggered control with time-varying network delays. In *Proceedings of the 50th IEEE Conference on Decision and Control and European Control Conference*, IEEE, Orlando, USA, pp. 1650–1655, 2011.
- [23] M. Miskowicz. Send-on-delta concept: An event-based data reporting strategy. *Sensors*, vol. 6, no. 1, pp. 49–63, 2006.
- [24] L. Zou, Z. D. Wang, H. J. Gao, X. H. Liu. Event-triggered state estimation for complex networks with mixed time delays via sampled data information: The continuous-time case. *IEEE Transactions on Cybernetics*, vol. 45, no. 12, pp. 2804–2815, 2015.
- [25] V. H. Nguyen, Y. S. Suh. Networked estimation for event-based sampling systems with packet dropouts. *Sensors*, vol. 9, no. 4, pp. 3078–3089, 2009.
- [26] D. E. Quevedo, V. Gupta, W. J. Ma, S. Yüksel. Stochastic stability of event-triggered anytime control. *IEEE Transactions on Automatic Control*, vol. 59, no. 12, pp. 3373–3379, 2014.
- [27] S. H. Mousavi, M. Ghodrati, H. J. Marquez. Integral-based event-triggered control scheme for a general class of nonlinear systems. *IET Control Theory & Applications*, vol. 9, no. 13, pp. 1982–1988, 2015.
- [28] E. Penovi, S. Maestri, R. G. Retegui, N. Wassinger, M. Benedetti. Event-based control system suitable for high-precision pulsed current source applications with improved switching behavior. *IEEE Transactions on Industrial Informatics*, vol. 11, no. 4, pp. 987–996, 2015.
- [29] D. Yue, E. Tian, Q. L. Han. A delay system method for designing event-triggered controllers of networked control systems. *IEEE Transactions on Automatic Control*, vol. 58, no. 2, pp. 475–481, 2013.
- [30] C. De Persis, R. Sailer, F. Wirth. Parsimonious event-triggered distributed control: A Zeno free approach. *Automatica*, vol. 49, no. 7, pp. 2116–2124, 2013.
- [31] D. R. Ding, Z. D. Wang, B. Shen, G. L. Wei. Event-triggered consensus control for discrete-time stochastic multi-agent systems: The input-to-state stability in probability. *Automatica*, vol. 62, pp. 284–291, 2015.
- [32] J. L. Xiong, J. Lam. Stabilization of linear systems over networks with bounded packet loss. *Automatica*, vol. 43, no. 1, pp. 80–87, 2007.
- [33] D. Wu, X. M. Sun, Y. Tan, W. Wang. On designing event-triggered schemes for networked control systems subject to one-step packet dropout. *IEEE Transactions on Industrial Informatics*, vol. 12, no. 3, pp. 902–910, 2016.
- [34] L. J. Zha, J. A. Fang, J. L. Liu. Two channel event-triggering communication schemes for networked control systems. *Neurocomputing*, vol. 197, pp. 45–52, 2016.
- [35] C. Peng, J. Zhang. Event-triggered output-feedback  $\infty$  control for networked control systems with time-varying sampling. *IET Control Theory & Applications*, vol. 9, no. 9, pp. 1384–1391, 2015.
- [36] H. J. Wang, Y. J. Ying, R. Q. Lu, A. K. Xue. Network-based  $H_\infty$  control for singular systems with event-triggered sampling scheme. *Information Sciences*, vol. 329, pp. 540–551, 2016.

- [37] P. Shi, H. J. Wang, C. C. Lim. Network-based event-triggered control for singular systems with quantizations. *IEEE Transactions on Industrial Electronics*, vol. 63, no. 2, pp. 1230–1238, 2016.
- [38] A. Selivanov, E. Fridman. Event-triggered  $H_\infty$  control: A switching approach. *IEEE Transactions on Automatic Control*, vol. 61, no. 10, pp. 3221–3226, 2016.
- [39] Y. Wang, W. Wang, G. P. Liu.  $H_\infty$  control of networked control systems based on event-time-driven model. *International Journal of Systems Science*, vol. 42, no. 10, pp. 1735–1745, 2011.
- [40] S. B. Li, D. Sauter, B. G. Xu. Co-design of event-triggered  $H_\infty$  control for discrete-time linear parameter-varying systems with network-induced delays. *Journal of the Franklin Institute*, vol. 352, no. 5, pp. 1867–1892, 2015.
- [41] S. Hu, Y. Zhang, Z. Du. Network-based  $H_\infty$  tracking control with event-triggering sampling scheme. *IET Control Theory & Applications*, vol. 6, no. 4, pp. 533–544, 2012.
- [42] S. L. Hu, D. Yue, X. P. Xie, Z. P. Du. Event-triggered  $H_\infty$  stabilization for networked stochastic systems with multiplicative noise and network-induced delays. *Information Sciences*, vol. 299, pp. 178–197, 2015.
- [43] A. K. Xue, H. J. Wang, R. Q. Lu. Event-based  $H_\infty$  control for discrete Markov jump systems. *Neurocomputing*, vol. 190, no. C, pp. 165–171, 2016.
- [44] H. C. Yan, T. T. Wang, H. Zhang, H. B. Shi. Event-triggered  $H_\infty$  control for uncertain networked T-S fuzzy systems with time delay. *Neurocomputing*, vol. 157, pp. 273–279, 2015.
- [45] E. Garcia, P. J. Antsaklis. Model-based event-triggered control for systems with quantization and time-varying network delays. *IEEE Transactions on Automatic Control*, vol. 58, no. 2, pp. 422–434, 2013.
- [46] D. Antunes, W. P. M. H. Heemels. Rollout event-triggered control: Beyond periodic control performance. *IEEE Transactions on Automatic Control*, vol. 59, no. 12, pp. 3296–3311, 2014.
- [47] A. Adaldo, F. Alderisio, D. Liuzza, G. D. Shi, D. V. Dimarogonas, M. di Bernardo, K. H. Johansson. Event-triggered pinning control of switching networks. *IEEE Transactions on Control of Network Systems*, vol. 2, no. 2, pp. 204–213, 2015.
- [48] N. He, D. W. Shi. Event-based robust sampled-data model predictive control: A non-monotonic Lyapunov function approach. *IEEE Transactions on Circuits and Systems I: Regular Papers*, vol. 62, no. 10, pp. 2555–2564, 2015.
- [49] A. Ferrara, S. Sacone, S. Siri. Design of networked freeway traffic controllers based on event-triggered control concepts. *International Journal of Robust and Nonlinear Control*, vol. 26, no. 6, pp. 1162–1183, 2016.
- [50] A. Selivanov, E. Fridman. Distributed event-triggered control of diffusion semilinear PDEs. *Automatica*, vol. 68, pp. 344–351, 2016.
- [51] Z. J. Wu, Q. S. Jia, X. H. Guan. Optimal control of multiroom HVAC system: An event-based approach. *IEEE Transactions on Control Systems Technology*, vol. 24, no. 2, pp. 662–669, 2016.
- [52] W. Wu, S. Reimann, D. Görges, S. Liu. Suboptimal event-triggered control for time-delayed linear systems. *IEEE Transactions on Automatic Control*, vol. 60, no. 5, pp. 1386–1391, 2015.
- [53] K. Duan, W. D. Zhang. Event-triggered fault-tolerant control for networked systems with dynamic quantiser. *IET Control Theory & Applications*, vol. 10, no. 9, pp. 1088–1096, 2016.
- [54] L. Y. Zhang, M. Z. Q. Chen. Event-triggered control for semi-global stabilisation of systems with actuator saturation. *International Journal of Control*, vol. 89, no. 5, pp. 1047–1064, 2016.
- [55] A. Sahoo, H. Xu, S. Jagannathan. Neural network-based event-triggered state feedback control of nonlinear continuous-time systems. *IEEE Transactions on Neural Networks and Learning Systems*, vol. 27, no. 3, pp. 497–509, 2016.
- [56] X. X. Yin, D. Yue, S. L. Hu. Model-based event-triggered predictive control for networked systems with communication delays compensation. *International Journal of Robust and Nonlinear Control*, vol. 25, no. 18, pp. 3572–3595, 2015.
- [57] S. Al-Areqi, D. Görges, S. Liu. Event-based control and scheduling codesign: stochastic and robust approaches. *IEEE Transactions on Automatic Control*, vol. 60, no. 5, pp. 1291–1303, 2015.
- [58] S. Al-Areqi, D. Görges, S. Liu. Event-based networked control and scheduling codesign with guaranteed performance. *Automatica*, vol. 57, pp. 128–134, 2015.
- [59] A. Girard. Dynamic triggering mechanisms for event-triggered control. *IEEE Transactions on Automatic Control*, vol. 60, no. 7, pp. 1992–1997, 2015.
- [60] C. Liu, F. Hao. Dynamic output-feedback control for linear systems by using event-triggered quantisation. *IET Control Theory & Applications*, vol. 9, no. 8, pp. 1254–1263, 2015.
- [61] T. F. Liu, Z. P. Jiang. Event-based control of nonlinear systems with partial state and output feedback. *Automatica*, vol. 53, pp. 10–22, 2015.
- [62] H. Yu, F. Hao. A Lyapunov-based small-gain approach on design of triggering conditions in event-triggered control systems. *International Journal of Robust and Nonlinear Control*, vol. 26, no. 13, pp. 2938–2960, 2016.
- [63] D. W. Zhang, Q. L. Han, X. C. Jia. Network-based output tracking control for T-S fuzzy systems using an event-triggered communication scheme. *Fuzzy Sets and Systems*, vol. 273, pp. 26–48, 2015.
- [64] C. Peng, Q. L. Han. A novel event-triggered transmission scheme and  $\mathcal{L}_2$  control co-design for sampled-data control systems. *IEEE Transactions on Automatic Control*, vol. 58, no. 10, pp. 2620–2626, 2013.

- [65] X. Y. Meng, T. W. Chen. Event detection and control co-design of sampled-data systems. *International Journal of Control*, vol. 87, no. 4, pp. 777–786, 2014.
- [66] H. Yu, F. Hao. Design of event conditions in event-triggered control systems: a non-fragile control system approach. *IET Control Theory & Applications*, vol. 10, no. 9, pp. 1069–1077, 2016.
- [67] J. F. Wu, Q. S. Jia, K. H. Johansson, L. Shi. Event-based sensor data scheduling: Trade-off between communication rate and estimation quality. *IEEE Transactions on Automatic Control*, vol. 58, no. 4, pp. 1041–1046, 2013.
- [68] V. H. Nguyen. Performance analysis of state estimation problem over network applying event-based sampling scheme. In *Proceedings of International Conference on Control, Automation and Information Sciences*, IEEE, Ho Chi Minh City, Vietnam, pp. 283–287, 2012.
- [69] D. W. Shi, T. W. Chen, L. Shi. An event-triggered approach to state estimation with multiple point- and set-valued measurements. *Automatica*, vol. 50, no. 6, pp. 1641–1648, 2014.
- [70] S. Trimpe, R. D’Andrea. Event-based state estimation with variance-based triggering. *IEEE Transactions on Automatic Control*, vol. 59, no. 12, pp. 3266–3281, 2014.
- [71] J. Sijs, B. Noack, U. D. Hanebeck. Event-based state estimation with negative information. In *Proceedings of the 16th International Conference on Information Fusion*, IEEE, Istanbul, Turkey, pp. 2192–2199, 2013.
- [72] H. L. Dong, Z. D. Wang, S. X. Ding, H. J. Gao. Event-based  $H_\infty$  filter design for a class of nonlinear time-varying systems with fading channels and multiplicative noises. *IEEE Transactions on Signal Processing*, vol. 63, no. 13, pp. 3387–3395, 2015.
- [73] D. W. Shi, T. W. Chen, L. Shi. On set-valued Kalman filtering and its application to event-based state estimation. *IEEE Transactions on Automatic Control*, vol. 60, no. 5, pp. 1275–1290, 2015.
- [74] Y. F. Lin, Q. L. Han, F. W. Yang, D. Jarvis. Event-triggered  $H_\infty$  filtering for networked systems based on network dynamics. In *Proceedings of the 39th Annual Conference of IEEE Industrial Electronics Society*, IEEE, Vienna, Austria, pp. 5638–5643, 2013.
- [75] C. Peng, M. R. Fei. Networked  $H_\infty$  filtering for discrete linear systems with a periodic event-triggering communication scheme. *IET Signal Processing*, vol. 7, no. 8, pp. 754–765, 2013.
- [76] X. M. Zhang, Q. L. Han. Event-based  $H_\infty$  filtering for sampled-data systems. *Automatica*, vol. 51, pp. 55–69, 2015.
- [77] X. M. Zhang, Q. L. Han. On designing event-based  $H_\infty$  filters for sampled-data systems. In *Proceedings of the 51st Annual Conference on Decision and Control*, IEEE, Maui, USA, pp. 6048–6053, 2012.
- [78] H. L. Dong, Z. D. Wang, D. R. Ding. Event-based filtering for discrete time-varying systems. In *Proceedings of 20th International Conference on Automation and Computing*, IEEE, Cranfield, UK, pp. 116–121, 2014.
- [79] J. L. Liu, Q. H. Liu, J. Cao, Y. Y. Zhang. Adaptive event-triggered  $H_\infty$  filtering for T-S fuzzy system with time delay. *Neurocomputing*, vol. 189, pp. 86–94, 2016.
- [80] H. J. Wang, P. Shi, R. K. Agarwal. Network-based event-triggered filtering for Markovian jump systems. *International Journal of Control*, vol. 89, no. 6, pp. 1096–1110, 2016.
- [81] J. Zhang, C. Peng. Event-triggered  $H_\infty$  filtering for networked Takagi-Sugeno fuzzy systems with asynchronous constraints. *IET Signal Processing*, vol. 9, no. 5, pp. 403–411, 2015.
- [82] J. L. Liu, D. Yue. Event-based fault detection for networked systems with communication delay and nonlinear perturbation. *Journal of the Franklin Institute*, vol. 350, no. 9, pp. 2791–2807, 2013.
- [83] M. A. Sid, S. Aberkane, D. Maquin, D. Sauter. Fault detection of event based control system. In *Proceedings of the 22nd Mediterranean Conference of Control and Automation*, IEEE, Palermo, Italy, pp. 452–458, 2014.
- [84] Y. L. Wang, P. Shi, C. C. Lim, Y. Liu. Event-triggered fault detection filter design for a continuous-time networked control system. *IEEE Transactions on Cybernetics*, vol. 46, no. 12, pp. 3414–3426, 2016.
- [85] S. B. Li, D. Sauter, B. G. Xu. Fault isolation filter for networked control system with event-triggered sampling scheme. *Sensors*, vol. 11, no. 1, pp. 557–572, 2011.
- [86] Y. Liu, Z. D. Wang, X. He, D. H. Zhou. Event-triggered fault estimation for nonlinear systems with missing measurements. In *Proceedings of the 33rd Chinese Control Conference*, IEEE, Nanjing, China, pp. 5533–5538, 2014.
- [87] M. S. Mahmoud, M. Sabih. Experimental investigations for distributed networked control systems. *IEEE Systems Journal*, vol. 8, no. 3, pp. 717–725, 2014.
- [88] M. S. Mahmoud, M. Sabih, M. Elshafei. Event-triggered output feedback control for distributed networked systems. *ISA Transactions*, vol. 60, pp. 294–302, 2016.
- [89] Q. Y. Liu, Z. D. Wang, X. He, D. H. Zhou. Event-based  $H_\infty$  consensus control of multi-agent systems with relative output feedback: The finite-horizon case. *IEEE Transactions on Automatic Control*, vol. 60, no. 9, pp. 2553–2558, 2015.
- [90] X. Chen, F. Hao. Event-triggered average consensus control for discrete-time multi-agent systems. *IET Control Theory & Applications*, vol. 6, no. 16, pp. 2493–2498, 2012.
- [91] Y. Fan, G. Feng, Y. Wang, C. Song. Distributed event-triggered control of multi-agent systems with combinatorial measurements. *Automatica*, vol. 49, no. 2, pp. 671–675, 2013.
- [92] G. S. Seyboth, D. V. Dimarogonas, K. H. Johansson. Event-based broadcasting for multi-agent average consensus. *Automatica*, vol. 49, no. 1, pp. 245–252, 2013.
- [93] X. Y. Meng, T. W. Chen. Event based agreement protocols for multi-agent networks. *Automatica*, vol. 49, no. 7, pp. 2125–2132, 2013.

- [94] X. X. Yin, D. Yue. Event-triggered tracking control for heterogeneous multi-agent systems with Markov communication delays. *Journal of the Franklin Institute*, vol. 350, no. 5, pp. 1312–1334, 2013.
- [95] X. F. Wang, M. D. Lemmon. Event-triggering in distributed networked control systems. *IEEE Transactions on Automatic Control*, vol. 56, no. 3, pp. 586–601, 2011.
- [96] G. Guo, L. Ding, Q. L. Han. A distributed event-triggered transmission strategy for sampled-data consensus of multi-agent systems. *Automatica*, vol. 50, no. 5, pp. 1489–1496, 2014.
- [97] C. X. Dou, B. Liu, J. M. Guerrero. Event-triggered hybrid control based on multi-agent system for microgrids. *IET Generation, Transmission & Distribution*, vol. 8, no. 12, pp. 1987–1997, 2014.
- [98] X. Chen, F. Hao, A. Rahmani. Asynchronous decentralised event-triggered control of multi-agent systems. *International Journal of Control*, vol. 87, no. 10, pp. 2130–2139, 2014.
- [99] H. J. Li, C. Ming, S. G. Shen, W. K. Wong. Event-triggered control for multi-agent systems with randomly occurring nonlinear dynamics and time-varying delay. *Journal of the Franklin Institute*, vol. 351, no. 5, pp. 2582–2599, 2014.
- [100] H. Zhang, G. Feng, H. C. Yan, Q. J. Chen. Observer-based output feedback event-triggered control for consensus of multi-agent systems. *IEEE Transactions on Industrial Electronics*, vol. 61, no. 9, pp. 4885–4894, 2014.
- [101] H. Q. Li, X. F. Liao, T. W. Huang, W. Zhu. Event-triggering sampling based leader-following consensus in second-order multi-agent systems. *IEEE Transactions on Automatic Control*, vol. 60, no. 7, pp. 1998–2003, 2015.
- [102] P. Yu, L. Ding, Z. W. Liu, Z. H. Guan. Leader-follower flocking based on distributed event-triggered hybrid control. *International Journal of Robust and Nonlinear Control*, vol. 26, no. 1, pp. 143–153, 2016.
- [103] H. P. Zhang, D. Yue, X. X. Yin, S. L. Hu, C. X. Dou. Finite-time distributed event-triggered consensus control for multi-agent systems. *Information Sciences*, vol. 339, pp. 132–142, 2016.
- [104] Y. Cheng, V. Ugrinovskii. Event-triggered leader-following tracking control for multivariable multi-agent systems. *Automatica*, vol. 70, pp. 204–210, 2016.
- [105] N. K. Mu, X. F. Liao, T. W. Huang. Consensus of second-order multi-agent systems with random sampling via event-triggered control. *Journal of the Franklin Institute*, vol. 353, no. 6, pp. 1423–1435, 2016.
- [106] T. Y. Wang, L. Y. Chang, P. Y. Chen. A collaborative sensor-fault detection scheme for robust distributed estimation in sensor networks. *IEEE Transactions on Communications*, vol. 57, no. 10, pp. 3045–3058, 2009.
- [107] J. Teng, H. Snoussi, C. Richard. Collaborative multi-target tracking in wireless sensor networks. *International Journal of Systems Science*, vol. 42, no. 9, pp. 1427–1443, 2011.
- [108] R. Olfati-Saber. Distributed Kalman filtering for sensor networks. In *Proceedings of the 46th IEEE Conference on Decision and Control*, IEEE, New Orleans, USA, pp. 5492–5498, 2007.
- [109] D. R. Ding, Z. D. Wang, B. Shen, H. L. Dong. Event-triggered distributed  $\mathcal{H}_\infty$  state estimation with packet dropouts through sensor networks. *IET Control Theory & Applications*, vol. 9, no. 13, pp. 1948–1955, 2015.
- [110] L. Yan, X. M. Zhang, Z. J. Zhang, Y. J. Yang. Distributed state estimation in sensor networks with event-triggered communication. *Nonlinear Dynamics*, vol. 76, no. 1, pp. 169–181, 2014.
- [111] L. Ding, G. Guo. Distributed event-triggered  $H_\infty$  consensus filtering in sensor networks. *Signal Processing*, vol. 108, pp. 365–375, 2015.
- [112] X. Y. Meng, T. W. Chen. Optimality and stability of event triggered consensus state estimation for wireless sensor networks. In *Proceedings of the American Control Conference*, IEEE, Portland, USA, pp. 3565–3570, 2014.
- [113] H. L. Dong, Z. D. Wang, F. E. Alsaadi, B. Ahmad. Event-triggered robust distributed state estimation for sensor networks with state-dependent noises. *International Journal of General Systems*, vol. 44, no. 2, pp. 254–266, 2015.
- [114] Q. Y. Liu, Z. D. Wang, X. He, D. H. Zhou. Event-based distributed filtering with stochastic measurement fading. *IEEE Transactions on Industrial Informatics*, vol. 11, no. 6, pp. 1643–1652, 2015.
- [115] Q. Y. Liu, Z. D. Wang, X. He, D. H. Zhou. Event-based recursive distributed filtering over wireless sensor networks. *IEEE Transactions on Automatic Control*, vol. 60, no. 9, pp. 2470–2475, 2015.
- [116] X. H. Ge, Q. L. Han. Distributed event-triggered  $H_\infty$  filtering over sensor networks with communication delays. *Information Sciences*, vol. 291, pp. 128–142, 2015.
- [117] J. Hu, Z. D. Wang, J. L. Liang, H. L. Dong. Event-triggered distributed state estimation with randomly occurring uncertainties and nonlinearities over sensor networks: A delay-fractioning approach. *Journal of the Franklin Institute*, vol. 352, no. 9, pp. 3750–3763, 2015.
- [118] W. L. Li, Y. M. Jia, J. P. Du. Event-triggered Kalman consensus filter over sensor networks. *IET Control Theory & Applications*, vol. 10, no. 1, pp. 103–110, 2016.
- [119] G. L. Wei, S. Liu, L. C. Wang, Y. X. Wang. Event-based distributed set-membership filtering for a class of time-varying non-linear systems over sensor networks with saturation effects. *International Journal of General Systems*, vol. 45, no. 5, pp. 532–547, 2016.
- [120] J. H. Zhang, Y. M. Kuai, M. F. Ren, Z. L. Luo, M. M. Lin. Event-triggered distributed filtering for non-Gaussian systems over wireless sensor networks using survival information potential criterion. *IET Control Theory & Applications*, vol. 10, no. 13, pp. 1524–1530, 2016.
- [121] P. Millán, L. Orihuela, I. Jurado, C. Vivas, F. R. Rubio. Distributed estimation in networked systems under periodic and event-based communication policies. *International Journal of Systems Science*, vol. 46, no. 1, pp. 139–151, 2015.

- [122] J. Weimer, J. Araújo, K. H. Johansson. Distributed event-triggered estimation in networked systems. In *Proceedings of the 4th IFAC Conference on Analysis and Design of Hybrid Systems*, Elsevier, Eindhoven, Netherlands, pp. 178–185, 2012.
- [123] D. W. Shi, T. W. Chen, L. Shi. Event-triggered maximum likelihood state estimation. *Automatica*, vol. 50, no. 1, pp. 247–254, 2014.
- [124] W. P. M. H. Heemels, K. H. Johansson, P. Tabuada. An introduction to event-triggered and self-triggered control. In *Proceedings of the 51st Annual Conference on Decision and Control*, IEEE, Maui, USA, pp. 3270–3285, 2012.
- [125] J. F. Zhao, L. Y. Xiang, F. Chen, W. Y. Lan. Distributed consensus via self-triggered output feedback. *IET Control Theory & Applications*, vol. 10, no. 10, pp. 1170–1180, 2016.
- [126] D. Senejohnny, P. Tesi, C. De Persis. Self-triggered coordination over a shared network under denial-of-service. In *Proceedings of the 54th Annual Conference on Decision and Control*, IEEE, Osaka, Japan, pp. 3469–3474, 2015.
- [127] K. Hashimoto, S. Adachi, D. V. Dimarogonas. Self-triggered model predictive control for nonlinear input-affine dynamical systems via adaptive control samples selection. *IEEE Transactions on Automatic Control*, vol. 62, no. 1, pp. 177–189, 2017.
- [128] Y. Fan, L. Liu, G. Feng, Y. Wang. Self-triggered consensus for multi-agent systems with zeno-free triggers. *IEEE Transactions on Automatic Control*, vol. 60, no. 10, pp. 2779–2784, 2015.
- [129] V. S. Dolk, D. P. Borgers, W. P. M. H. Heemels. Output-based and decentralized dynamic event-triggered control with guaranteed  $L_p$ -gain performance and Zeno-freeness. *IEEE Transactions on Automatic Control*, vol. 62, no. 1, pp. 34–49, 2017.



**Lei Zou** received the B.Sc. degree in automation from Beijing Institute of Petrochemical Technology, China in 2008, the M.Sc. degree in control science and engineering from China University of Petroleum (Beijing Campus), China in 2011, and the Ph.D. degree in control science and engineering from Harbin Institute of Technology, China in 2016. From October 2013 to

October 2015, he was a visiting Ph.D. student with the Department of Computer Science, Brunel University London, UK. He is a very active reviewer for many international journals.

His research interests include nonlinear stochastic control and filtering, as well as networked control under various communication protocols.

E-mail: zouleicup@gmail.com  
ORCID iD: 0000-0002-0409-7941



**Zi-Dong Wang** received the B.Sc. degree in mathematics from Suzhou University, China in 1986, the M.Sc. degree in applied mathematics in 1990 and the Ph.D. degree in electrical engineering in 1994, both from Nanjing University of Science and Technology, China. He is currently a professor of dynamical systems and computing in the Department of Computer Science, Brunel University London, UK. From 1990 to 2002, he held teaching and research appointments in universities in China, Germany and UK. He has published more than 300 papers in refereed international journals. He is a holder of the Alexander von Humboldt Research Fellowship of Germany, the JSPS Research Fellowship of Japan, William Mong Visiting Research Fellowship of Hong Kong. He is a fellow of the IEEE. He is serving or has served as the editor-in-chief for *Neurocomputing*, an associate editor for 12 international journals, including *IEEE Transactions on Automatic Control*, *IEEE Transactions on Control Systems Technology*, *IEEE Transactions on Neural Networks*, *IEEE Transactions on Signal Processing*, and *IEEE Transactions on Systems, Man, and Cybernetics-Systems*. He is also a fellow of the Royal Statistical Society and a member of program committee for many international conferences.

His research interests include dynamical systems, signal processing, bioinformatics, control theory and applications.

E-mail: Zidong.Wang@brunel.ac.uk (Corresponding author)  
ORCID iD: 0000-0002-9576-7401



**Dong-Hua Zhou** received the B.Eng., M.Sc., and Ph.D. degrees in electrical engineering from Shanghai Jiaotong University, China in 1985, 1988, and 1990, respectively. He was an Alexander von Humboldt research fellow with the University of Duisburg, Germany from 1995 to 1996, and a visiting scholar with Yale university, USA from 2001 to 2002. He joined Tsinghua University, China in 1997, and was a professor and the head of the

Department of Automation, Tsinghua University, China from 2008 to 2015. He is now the vice president of Shandong University of Science and Technology, China. He has authored and coauthored over 140 peer-reviewed international journal papers and 6 monographs. He is a member of the IFAC Technical Committee on Fault Diagnosis and Safety of Technical Processes, a senior member of IEEE, an associate editor of *the Journal of Process Control*, the associate chairman of Chinese Association of Automation.

His research interests include fault diagnosis, fault-tolerant control, process control, networked control and filtering, and reliable control.

E-mail: zdh@mail.tsinghua.edu.cn